In Exercises 1–12, find the volume of the solid obtained by revolving each of the following regions about the y axis and sketch the region.

- 1. The region under the graph of  $\sin x$  on  $[0, \pi]$ .
- 2. The region under the graph of  $\cos 2x$  on  $[0, \pi/4]$ .
- 3. The region under the graph of  $2 (x 1)^2$  on [0, 2].
- 4. The region under the graph of  $\sqrt{4-4x^2}$  on [0, 1].
- 5. The region between the graphs of  $\sqrt{3-x^2}$  and 5+x on [0,1].
  - 6. The region between the graphs of  $\sin x$  and x on  $[0, \pi/2]$ .
- 7. The circular region with center (a, 0) and radius r (0 < r < a).
- 8. The circular region with radius 2 and center (6,0).