



Cinvestav

1/ 30

Luis J
Dominguez
Perez

Introduction

Matrices

Functions,
Procedures,
and Package.

Prime
numbers

Magma Tutorial for pairing cryptographers. Part I - Introduction

Luis J Dominguez Perez

Cinvestav, Mexico

September, 2011



Cinvestav

Table of contents

2/ 30

Luis J
Dominguez
Perez

Introduction

Matrices

Functions,
Procedures,
and Package.

Prime
numbers

1 Introduction

2 Matrices

3 Functions, Procedures, and Package.

4 Prime numbers



Cinvestav

Magma

3/ 30

Luis J
Dominguez
Perez

Introduction

Matrices

Functions,
Procedures,
and Package.

Prime
numbers



Cinvestav

The Magma shell

4/ 30

Luis J
Dominguez
Perez

Introduction

Matrices

Functions,
Procedures,
and Package.

Prime
numbers

- The typical way of running magma is using its interactive shell, which behaves similarly to those of Python, Perl or Sage.
- Magma does not provides a graphical interface, however, it is possible to integrate it into Sage to produce graphics.
- The command shell symbol is $>$, and the command delimiter is $;$.
- Since we are using a delimiter, we can have several commands in the same line.



Cinvestav

The Magma program

5/ 30

Luis J
Dominguez
Perez

Introduction

Matrices

Functions,
Procedures,
and Package.

Prime
numbers

- We can have several Magma copies of the program at the same time.
- Magma uses one and only one core per copy of the program.
- Each copy of Magma runs in a non-intrusive environment. (We can run 3 copies of Magma in a Quad core and still have a responsible system, which is useful for running a test with several set of inputs).

Arithmetic Operators

- Assignment :=
- $+$, $-$, $*$, $/$, \wedge , mod, div, cat, etc.
- $+$:=, $-$:=, $*$:=

Boolean operators

- eq, ne, not, and, or, in

For the Binary Operations, I convert the number into a string sequence of the bits.



Cinvestav

Hands-on

7 / 30

Luis J
Dominguez
Perez

Introduction

Matrices

Functions,
Procedures,
and Package.

Prime
numbers

Open magma and do the following exercise:

- $x \leftarrow 2$
- $y \leftarrow x$
- $x \leftarrow z$
- $z \leftarrow x^2$
- $a \leftarrow 1/2$
- $b \leftarrow a^{-1}$

Use “variable”; to display its value.

More printing

- `printf "A=%o\n",x; //as in c/c++`
- `Sprintf(" A=%o\n",x);`
- `PrintFile(" MyFile",Sprintf(" %o,%o\n",3,5));`

Use `"%h"` to display values in hexadecimal.

For

- for $i:=1$ to 10 do ... end for;
- for i in $[1..9]$ do ... end for;
- for $i:= 10$ to 1 by -1 do ... end for;

While

- while i lt 10 do ... end while;

Repeat until

- repeat ... until i lt 10;



Cinvestav

Conditionals

10/ 30

Luis J
Dominguez
Perez

Introduction

Matrices

Functions,
Procedures,
and Package.

Prime
numbers

if

- if i eq 10 then ... end if;
- if i eq true then ... else ... end if;
- if i eq 1 then ... elif i eq 0 then ... else ... end if;

switch

- case a: when: ... else: ... end case;



- **L:=Open**(" NOTICE" ," r");
- while true do
 - s:=**Gets**(L);
 - if **IsEof**(s) then break; end if;
 - print s;
- end while;
- **Flush**(L);

Magma will do the cleaning, but it is always better to explicitly close a file (specially when writing in it).



Cinvestav

Hands-on

12/ 30

Luis J
Dominguez
Perez

Introduction

Matrices

Functions,
Procedures,
and Package.

Prime
numbers

Exercise:

- Create a file with the multiplication tables.



The difference:

```
i:={IntegerRing() | 1,2,3}; i;
```

```
i:={IntegerRing() | 1,3,5}; i;
```

```
i:=[IntegerRing() | 1,5,3];
```

Autofilling it:

```
T := [ Integers() | x^2+x+1 :  
      x in { -3 .. 2 by 1 } ];
```

Accessing elements:

- `a[1][2];`
- `a[1,2];`

both are OK



More on sets and sequences

New operators:

- join
- meet
- cat

Modifying the set

- Append, Insert, Include, Exclude
- Prune, Remove
- Sort, Reverse, Rotate

Getting information

- Maximum, Minimum, #, Random, Index, Parent, Universe, Category, etc.



Generating a matrix:

```
Matrix(IntegerRing(), 2, 2, [0,0,0,0]);
```

```
Matrix(RationalField(), 5, 10, [<1,2,23>,  
    <3,7,11>, <5,10,-1>]);
```

```
Matrix(IntegerRing(), 10, 10, [<2*i-1, 2*j-1, i*j>:  
    i, j in [1..5]]);
```

Generation shortcuts:

- `ZeroMatrix(Ring,m,n)`
- `DiagonalMatrix(Ring,n,Sequence)`
- `ScalarMatrix(n,value)`
- `SymmetricMatrix(Sequence)`

Operators:

- `NumberOfRows`
- `NumberOfColumns`



Cinvestav

Hands-on

17 / 30

Luis J
Dominguez
Perez

Introduction

Matrices

Functions,
Procedures,
and Package.

Prime
numbers

Exercise:

- Create a file with the multiplication tables. (using matrices)



Two ways to declare a function:

- `f := function`
- `function f`

Both end with `end function`;

There's a difference though, one may need to use `$$` to write a recursive function.

Actually, there's a third one:

- `f := func< x | x^2 >`

The same principle applies for the procedure, exempt that:

- It does not `return` statements
- It supports parameters as reference ($\sim a$)

Optionally, we can forward a definition of a procedure with `forward f`;



Cinvestav

Hands-on

20/ 30

Luis J
Dominguez
Perez

Introduction

Matrices

Functions,
Procedures,
and Package.

Prime
numbers

Exercise:

- Create a function and a procedure to get the multiplication tables.



Cinvestav

Package I

21 / 30

Luis J
Dominguez
Perez

Introduction

Matrices

Functions,
Procedures,
and Package.

Prime
numbers

A package, is a function or procedure which will be compiled by Magma at loading time.

A package is much more faster than a regular function or procedure, since it requires the user to specify the data-types of the arguments.

We “Attach” or “Detach” at runtime the file containing our package.

The syntax is as follows:

```
intrinsic NAME(ARG-LIST) [ -> RET-LIST ]  
{ COMMENT-TEXT }  
statements  
end intrinsic;
```

For example:

```
intrinsic myGCD(x::RngIntElt, y::RngIntElt)  
-> RngIntElt  
{ Return the GCD of x and y }  
    return ...;  
end intrinsic;
```

Please note that the documentation **is mandatory**

An associative array is a type of array with a named index.
Useful for look up tables.

- `AssociativeArray`
- `Remove`
- `Keys`
- `IsDefined`



Cinvestav

Hands-on

24 / 30

Luis J
Dominguez
Perez

Introduction

Matrices

Functions,
Procedures,
and Package.

Prime
numbers

Exercise:

- Create a package with the multiplication tables as a lookup



Cinvestav

Prime numbers

25 / 30

Luis J
Dominguez
Perez

Introduction

Matrices

Functions,
Procedures,
and Package.

Prime
numbers

Generating a prime number

- NextPrime
- PreviousPrime
- NthPrime
- RandomPrime

Primality test:

- IsPrime
- IsProbablePrime
- IsPrimePower
- Factorisation



Cinvestav

Hands-on

26/ 30

Luis J
Dominguez
Perez

Introduction

Matrices

Functions,
Procedures,
and Package.

Prime
numbers

Exercises:

(write down a function to)

- Determine if a number is *almost* prime
- Compute the MCM of two numbers
- Compute the mcm of two numbers
- Compute the Euler totient function



Cinvestav

More hands-on

27 / 30

Luis J
Dominguez
Perez

Introduction

Matrices

Functions,
Procedures,
and Package.

Prime
numbers

Exercises:

- Toy-example of RSA

Verify:

$(a^e)^d \equiv a \pmod{n}$, $(a^d)^e \equiv a \pmod{n}$, and $a^{ed} \equiv a \pmod{n}$.
for any random a .

- `RandomPrime(100)`
- Setup e
- $d1 \leftarrow \text{InverseMod}(e, p-1)$
- $d2 \leftarrow \text{InverseMod}(e, q-1)$
- $\text{GCD}(p-1, q-1)$
- `TrialDivision(p-1)` for common factors
- $d1 \bmod \text{common factor}$
- $d := \text{CRT}([d1, d2], [p-1, (q-1) \text{ div common factor}])$ or
- $d := \text{InverseMod}(e, \text{LCM}(p-1, q-1));$



When magma encounters a runtime error, it stops the execution of the program; if the program was running for a long period of time, then this is catastrophic.

```
procedure always_fails(x)
    error Error(x);
end procedure;
try
    always_fails(1);
catch e
    error "Error",e'Object;
end try;
```

After catching a runtime error, Magma continues the execution of the program.



Cinvestav

End

30/ 30

Luis J
Dominguez
Perez

Introduction

Matrices

Functions,
Procedures,
and Package.

Prime
numbers

End of Part I

There's part II