

## 1. SET THEORY

**Stefan Geschke** *Free University of Berlin* A dual open coloring axiom

*abstract* I will discuss a dual of the version of the Open Coloring Axiom that was introduced by Abraham, Rubin, and Shelah and indicate how this dual OCA follows from a statement about continuous colorings on Polish spaces that is known to be consistent. I will also mention some consequences of the new axiom.

**Neil Hindman** *Howard University* Discrete  $n$ -tuples in Hausdorff spaces

*abstract* We investigate the following three questions: Let  $n \in \mathbb{N}$ . For which Hausdorff spaces  $X$  is it true that whenever  $\Gamma$  is an arbitrary (respectively finite to one) (respectively injective) function from  $\mathbb{N}^n$  to  $X$ , there must exist an infinite subset  $M$  of  $\mathbb{N}$  such that  $\Gamma[M^n]$  is discrete? Of course, if  $n = 1$  the answer to all three questions is “all of them”. For  $n \geq 2$  the answers to the second and third questions are the same; in the case  $n = 2$  that answer is “those for which there are only finitely many points which are the limit of injective sequences”. The answers to the remaining instances involve the notion of  $n$ -Ramsey limit. We show also that the class of spaces satisfying these discreteness conclusions for all  $n$  includes the class of  $F$ -spaces. In particular, it includes the Stone-Ćech compactification of any discrete space.

**Justin Tatch Moore** *Boise State University* Recent developments in basis problems

*abstract* I will present the following ZFC result.

Theorem: There is a hereditarily LindelĆf, non-separable space.

One immediate consequence is that the uncountable regular topological spaces do not have a three element basis. The combinatorial object which makes the construction work also gives a number of other examples. In particular it produces a binary relation  $R$  which is neither below  $\omega \cdot \omega_1$  nor above  $[\omega_1]^{<\omega}$  in the Tukey order. It also gives an example of a function  $c$  from  $\omega_1 \times \omega_1$  to  $\omega_1$  which takes all values on any product of uncountable sets.

**A.A. Salama** *Department of Mathematics - Faculty of Education - Suez -* Compactness in Fuzzy Topological Spaces

*abstract* The purpose of this paper is to introduce and studied the concept of  $\alpha$ -compactness in the light of the concept of  $\alpha$ -shading in a fuzzy setting. A characterization of  $\alpha$ -compactness is given by using the concept of  $\alpha$ -finite intersection property due to [1]. We define the notion of fuzzy  $T_2$ -space and by using it we give some properties of  $\alpha$ -compactness. Also the image and the inverse image of compactness under some types of functions are investigated. Keywords: Fuzzy topological spaces, fuzzy  $\alpha$ -compactness, fuzzy  $\alpha$ -compactness, fuzzy  $\alpha$ -near compactness, fuzzy  $\alpha$ -continuity, fuzzy weakly  $\alpha$ -continuity, fuzzy  $T_2$ -space, fuzzy  $\alpha$ -open sets.

**Juris Steprans** *York University* Combinatorial questions associated with cardinal invariants of measure

*abstract* The problem of obtaining models of set theory where all sets of reals of size  $\aleph_1$  are null yet there are sets of reals of cardinality  $\aleph_1$  that are not null with respect to other natural measures involves establishing combinatorial lemmas about finite measure spaces. These will be discussed.